

Title: Algebraic approach to equivariance of solutions for an iterative equation

Author(s): Weinian Zhang and Bing Xu

Describing the symmetry of a mapping by equivariance with respect to a linear transformation group, the reference [Proc. Roy. Soc. Edinburgh **A130** (2000), 1153–1163] gave the existence of equivariant solutions of the polynomial-like iterative equation under the action of topologically finitely generated subgroups of $GL(\mathbb{R})$ on \mathbb{R} and the orthogonal group $\mathbf{O}(N)$ on \mathbb{R}^N ($N \geq 2$). In this paper, based on the algebraic structure of closed subgroups of $GL(\mathbb{R})$, we prove the equivariance of solutions on \mathbb{R} with respect to closed subgroups of $GL(\mathbb{R})$ and extend the result of $\mathbf{O}(N)$ -equivariance of solutions to the group $\mathbf{O}(N) \times \langle c \mathcal{I}_N \rangle$ on \mathbb{R}^N .

Address:

Weinian Zhang
Yangtze Center of Mathematics and Department of Mathematics
Sichuan University
Chengdu, Sichuan 610064
P.R. China
Address:
Bing Xu
Yangtze Center of Mathematics and Department of Mathematics
Sichuan University
Chengdu, Sichuan 610064
P.R. China
E-mail: xb0408@yahoo.com.cn; xb0408@sohu.com