

**Title:** Parameter-independent structure in periodic orbits of an iterated function system on the real line

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For the iterated function system on  $\mathbb{R}$  comprising the maps f(x) = ax + 1 and g(x) = bx, with a > 0 and 0 < b < 1, we represent each *n*-cycle by the composition (or *word*) in *f* and *g* corresponding to the cycle's point of least magnitude (or *perigee*). These representations are partitioned into equivalence classes using simple combinatorial criteria. Associated with each *n*-cycle are *n* polynomials in *a* and *b* whose values at a special value of *a* are partially ordered. An example is given showing that, for fixed *b*, the perigee word of an *n*-cycle is a function of *a*; but the ordering of the polynomial values enables us to prove that the *maximal* perigee word in each equivalence class is independent of the parameters *a* and *b*.

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