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**Title:** Sincov's inequalities on topological spaces

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Assume that X is a non-empty set, and T and S are real or complex mappings defined on the product  $X \times X$ . Additive and multiplicative Sincov's equations are:

$$T(x,z) = T(x,y) + T(y,z), \quad x,y,z \in X$$

and

$$S(x,z) = S(x,y) \cdot S(y,z), \quad x,y,z \in X_{z}$$

respectively. In the present paper, we study three related inequalities. We begin with functional inequality

$$G(x,z) \le G(x,y) \cdot G(y,z), \quad x,y,z \in X,$$

and assume that X is a topological space and  $G: X \times X \to \mathbb{R}$  is a continuous mapping. In some our statements a considerably weaker regularity than continuity of G is needed. Next, we study the reverse inequality:

$$F(x,z) \ge F(x,y) \cdot F(y,z), \quad x,y,z \in X,$$

as well as the additive inequality:

$$H(x,z) \le H(x,y) + H(y,z), \quad x,y,z \in X.$$

A corollary for generalized metric is derived.

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